

ECON 1550 International Finance

# Output and the Exchange Rate in the Short Run

# Behavioral equations in the goods market

$$Y = C + I + G + CA$$

$$\begin{array}{l} \text{DEMAND FOR} \\ \text{DOMESTIC} \\ \text{GOOD} \end{array} = C + I + G + CA$$

$$\begin{array}{l} \text{SUPPLY FOR} \\ \text{DOMESTIC} \\ \text{GOOD} \end{array} = Y$$

# Demand for domestic goods

$$\begin{array}{l} \text{DEMAND} \\ \text{FOR DOM} \\ \text{GOODS} \end{array} = C + I + G + CA = D$$

$$\begin{array}{l} \text{DOMESTIC} \\ \text{DEMAND} \\ \text{FOR GOODS} \end{array} \equiv A = C + I + G$$

$$A + EX - IM = A + CA = D$$

# Demand for domestic goods

$$C = C(Y_D^{(+1)}) \quad \text{CONSUMPTION (OF DOM. AND FOREIGN)}$$

$$Y_D \equiv Y - T \quad \text{DISPOSABLE INCOME}$$

$$I = \bar{I} \quad \text{EXOGENOUS INVESTMENT}$$

$$G = \bar{G} \quad \text{GOV. PURCHASES}$$

} BOTH DOM  
AND FOR.  
GOODS

$$CA = CA(q, Y - T, Y^*)$$

$$q \equiv \frac{EP^*}{P} = \frac{\text{DOLLAR PRICE OF FOREIGN GOOD}}{\text{DOLLAR PRICE OF DOM GOOD}}$$

# Demand for domestic goods

$$CA = EX - IM$$

$$EX = EX(q, Y^*)$$

(+1)   (+1)

$$IM = IM(q, Y_D)$$

(-)   (+1)

$q \uparrow$  VOLUME  $\downarrow$  PRICE  $q \uparrow$   
VOLUME DOMINATES

$q \uparrow$  REAL DEPR.

$$\frac{EP^*}{P} = q$$

$\Rightarrow$  HOME  
GOOD  
APPEARS  
CHEAPER

$$\underbrace{IM}_{\text{DOM GOOD}} = \underbrace{\frac{\text{PRICE}}{\text{FOREIGN GOOD}}}_{\equiv q} \times \underbrace{VOLUME}_{\text{FOREIGN GOOD}}$$

# A short-run model of the goods market

## Exogenous variables

Variable	Description
$E$	Nominal exchange rate
$I$	Investment
$G$	Government spending
$T$	Taxes
$P$	Price level
$P^*$	Foreign price level
$Y^*$	Foreign income

## Endogenous variables

Variable	Description	Equation	Type of equation
$Y$	Income, production	$Y = D$	Equilibrium condition
$Y_D$	Disposable income	$Y_D \equiv Y - T$	Identity
EX	Exports	$EX = EX(q, Y^*)$ <small>(+) (+)</small>	Behavioral
IM	Imports	$IM = IM(q, Y_D)$ <small>(-) (+)</small>	Behavioral
CA	Current account	$CA \equiv EX - IM = CA(q, Y_D, Y^*)$ <small>(+) (-) (+)</small>	Identity
$D$	Demand for domestic goods	$D \equiv C + I + G + CA$	Identity
$A$	Domestic demand	$A \equiv C + I + G$	Identity
$C$	Consumption	$C = C(Y_D)$ <small>(+)</small>	Behavioral
$q$	Real exchange rate	$q \equiv \frac{EP^*}{P}$	Identity

# DD Curve

$$Y = D$$

$$Y = C + I + G + CA$$

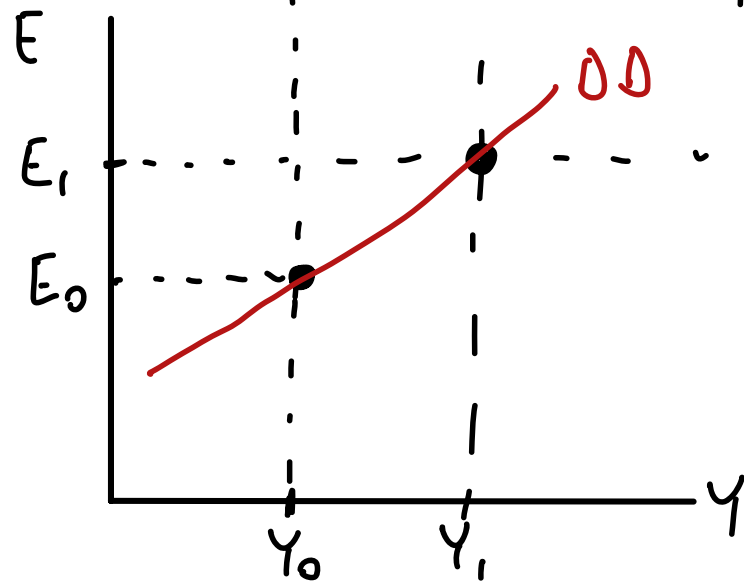
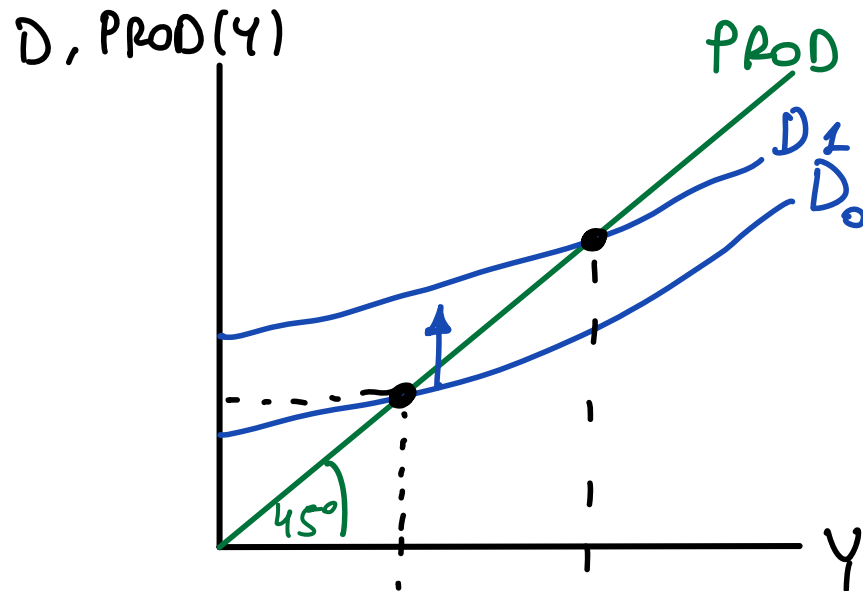
$$Y = C(Y_D) + I + G + CA(q, Y_D, Y^*)$$

(+)
(+)
(-)
(+)

$$Y = C(Y_D) + I + G + CA(EP^*/P, Y_D, Y^*)$$

(+)
(+)
(+)
(-)
(+)

$Y \uparrow$   $C \uparrow$  BUT  $CA \downarrow$ . HOWEVER,  
 $D$  ALWAYS  $\uparrow$



$$D = C + I + G + NX \quad \text{WHEN } Y \uparrow$$

$C \uparrow$   $NX \downarrow$  SO  $D$ ?

NOT UNCLEAR,  $D \uparrow$

$C$ : CONS. OF DOM. AND FOREIGN GOODS

$C - IM = \text{DOM DEM. FOR DOM GOOD}$

$$NX = \underbrace{EX}_{\text{DOES NOT CHANGE}} - \underbrace{IM}_{\text{IM GOES UP}} \quad \left| \quad \begin{aligned} C &= C_{\text{DOM GOOD}} + C_{\text{FOREIGN GOOD}} \\ IM &= \text{DOM DEMAND FOR FOREIGN} \end{aligned}$$

# Short-run FX and money market model

## Exogenous variables

Variable	Description
$R^*$	Foreign interest rate
$E^e$	Expected exchange rate
$Y$	Real income
$M^s$	Money supply
$P$	Price level

## Endogenous variables

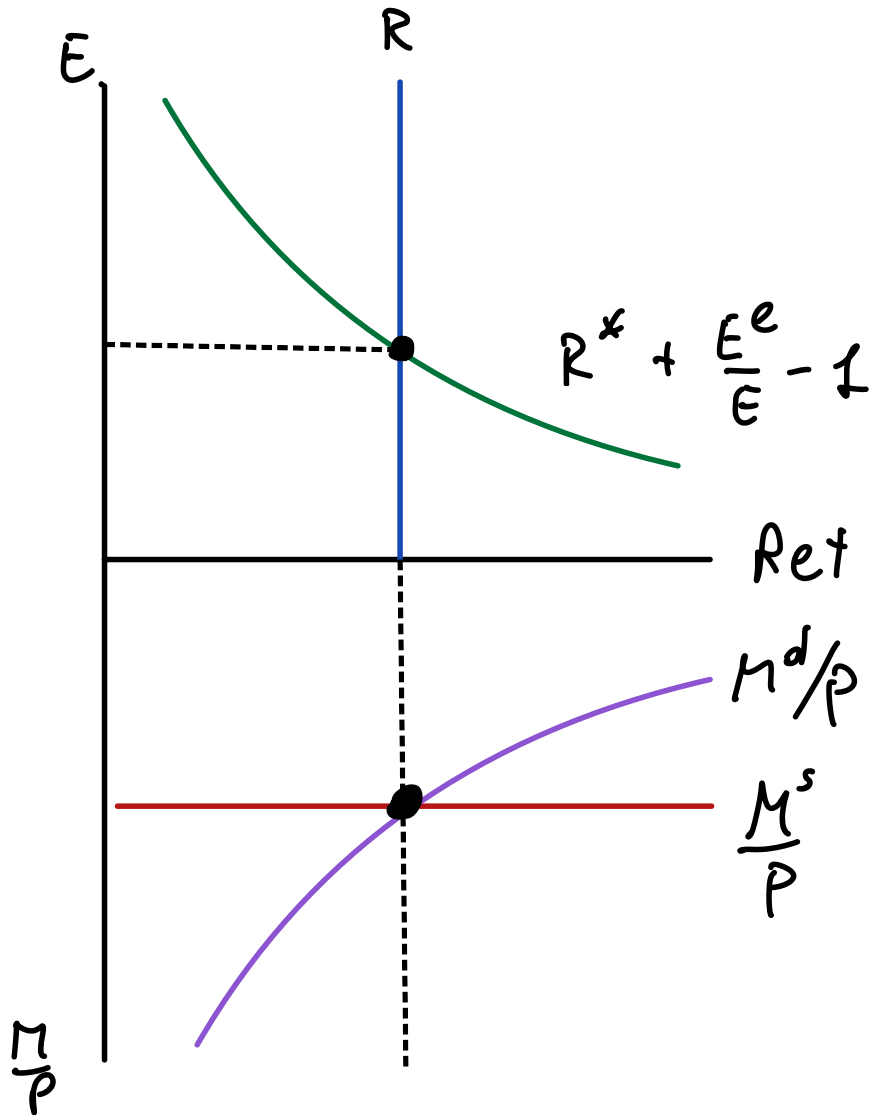
Variable	Description	Equation	Type of equation
$E$	Exchange rate	$R = R^* + \frac{E^e - E}{E}$	Equilibrium condition
$R$	Domestic interest rate	$M^d/P = L(R, Y)$	Behavioral equation
$M^d$	Money demand	$M^d = M^s$	Equilibrium condition

# AA Curve

(UIP): 
$$R = R^* + \frac{E^e}{E} - 1$$

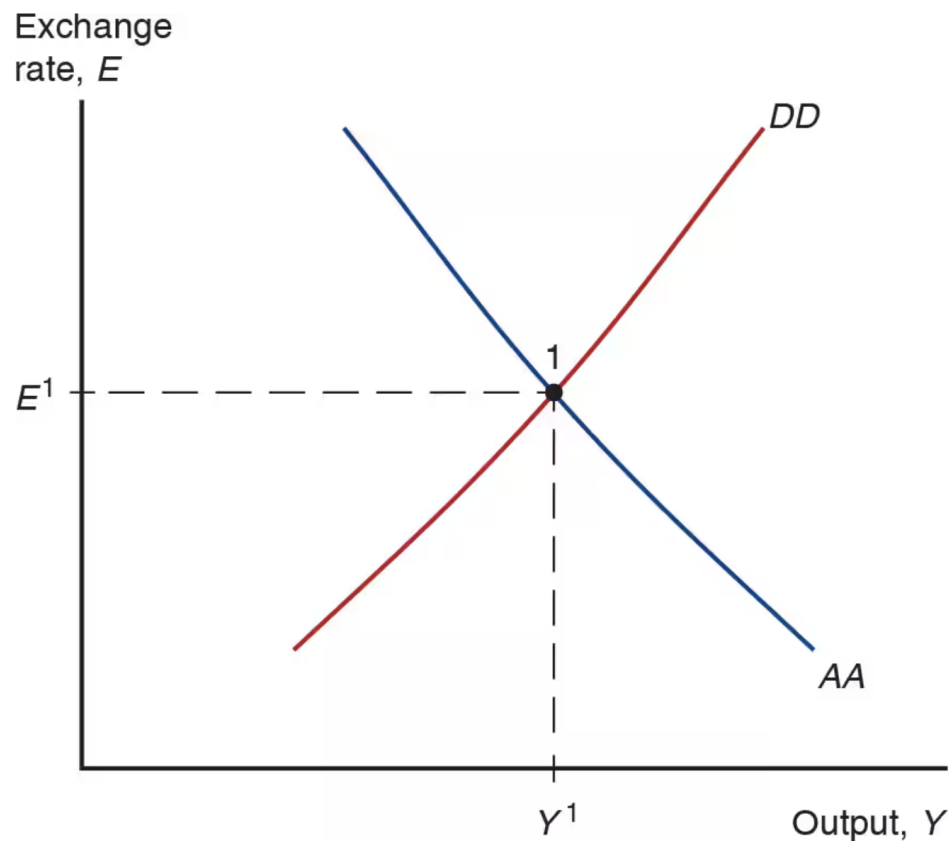
(MS) = (MD): 
$$\frac{M^s}{P} = L(R, Y)$$
  
 (-) (+)

Y EXO } FIND E FOR  
 E ENDO } GIVEN Y





# Short-run Equilibrium in *AA-DD* model



GOODS

$E$  EXO

MM + FX

$Y$  EXO

COMBINE

$Y, E$  ARE

BOTH

ENDO

# Example: DD Schedule

$$C(Y_D) = 1 + 0.75Y_D$$

(+)

$$EX(q, Y^*) = 0.15 + 0.5q + 0.1Y^*$$

(+)

$$IM(q, Y_D) = 0.1 - 0.2q + 0.12Y_D$$

(-)

$$Y_D = Y - T$$

$$q = \frac{EP^*}{P}$$

How to find the DD schedule

EQ. COND FOR GOODS:

$$Y = D$$

$$Y = C + I + G + CA$$

$$Y = 1 + 0.75(Y - T) + I + G + 0.15 + 0.5q + 0.1Y^* - 0.1 + 0.2q - 0.12(Y - T)$$

# Example: DD Schedule

. CAN SOLVE FOR E  
TO GET EXPLICIT

E = FUNCTION OF Y.

$$C(Y_D) = 1 + 0.75Y_D$$

(+)

$$EX(q, Y^*) = 0.15 + 0.5q + 0.1Y^*$$

(+)

$$IM(q, Y_D) = 0.1 - 0.2q + 0.12Y_D$$

(-)

$$Y_D = Y - T$$

$$q = \frac{EP^*}{P}$$

How to find the DD schedule

$$Y = 1 + 0.75(Y - T) + I + G +$$

$$+ 0.15 + 0.5q + 0.1Y^*$$

$$- 0.1 + 0.2q - 0.12(Y - T)$$

$$Y = 1 + 0.15 - 0.1 + I + G$$

$$(0.75 - 0.12)(Y - T) +$$

$$(0.5 + 0.2) \frac{EP^*}{P} + 0.1Y^*$$

# Example: AA Schedule

• CAN SOLVE FOR  $E$   
TO GET:

$E = \text{FUNCTION OF } Y$

$$R = R^* + \frac{E^e - E}{E}$$

$$\frac{M^d}{P} = \frac{M^s}{P}$$

$$\begin{aligned} \frac{M^d}{P} &= L\left(\underset{(-)}{R}, \underset{(+)}{Y}\right) \\ &= 1.1 - R + 0.05Y \end{aligned}$$

How to find the AA schedule

$$\frac{M^s}{P} = \frac{M^d}{P}$$

$$\frac{M^s}{P} = 1.1 - R + 0.05Y$$

$$\frac{M^s}{P} = 1.1 - R^* - \frac{E^e}{E} + 1 + 0.05Y$$

# Example: AA Schedule

• CAN SOLVE FOR  $E$   
TO GET:

$E = \text{FUNCTION OF } Y$

$$R = R^* + \frac{E^e - E}{E}$$

How to find the AA schedule

$$\frac{M^d}{P} = \frac{M^s}{P}$$

$$\frac{M^s}{P} = 1.1 - R^* - \frac{E^e}{E} + 1 + 0.5Y$$

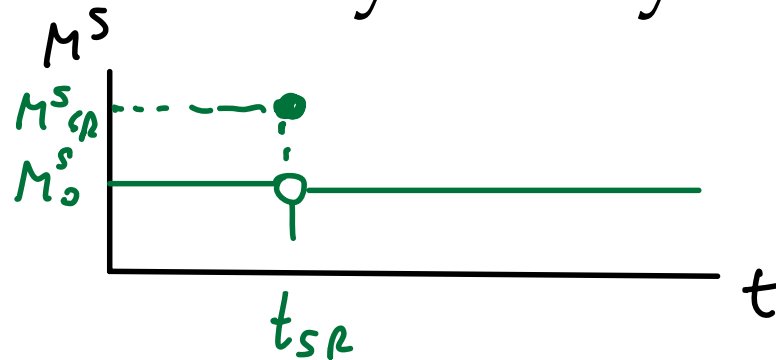
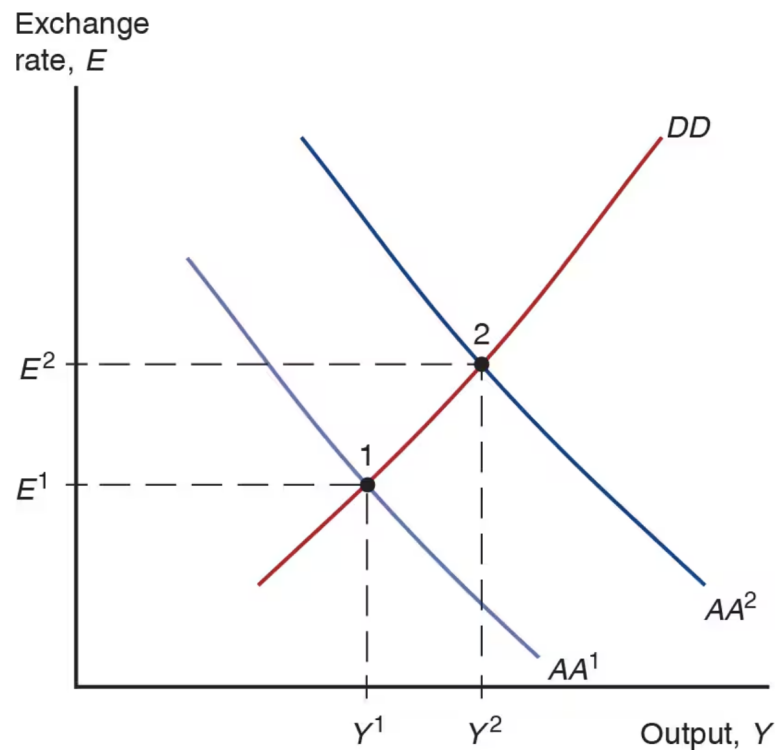
$$\begin{aligned} \frac{M^d}{P} &= L(\underset{(-)}{R}, \underset{(+)}{Y}) \\ &= 1.1 - R + 0.05Y \end{aligned}$$

SOLVE FOR  $E$ :

$$E^e/E = 1.1 - R^* + 1 - M^s/P + 0.5Y$$

$$E = \frac{E^e}{1.1 - R^* + 1 - M^s/P + 0.5Y}$$

# Temporary Change in Monetary Policy



TEMPORARY SHOCKS

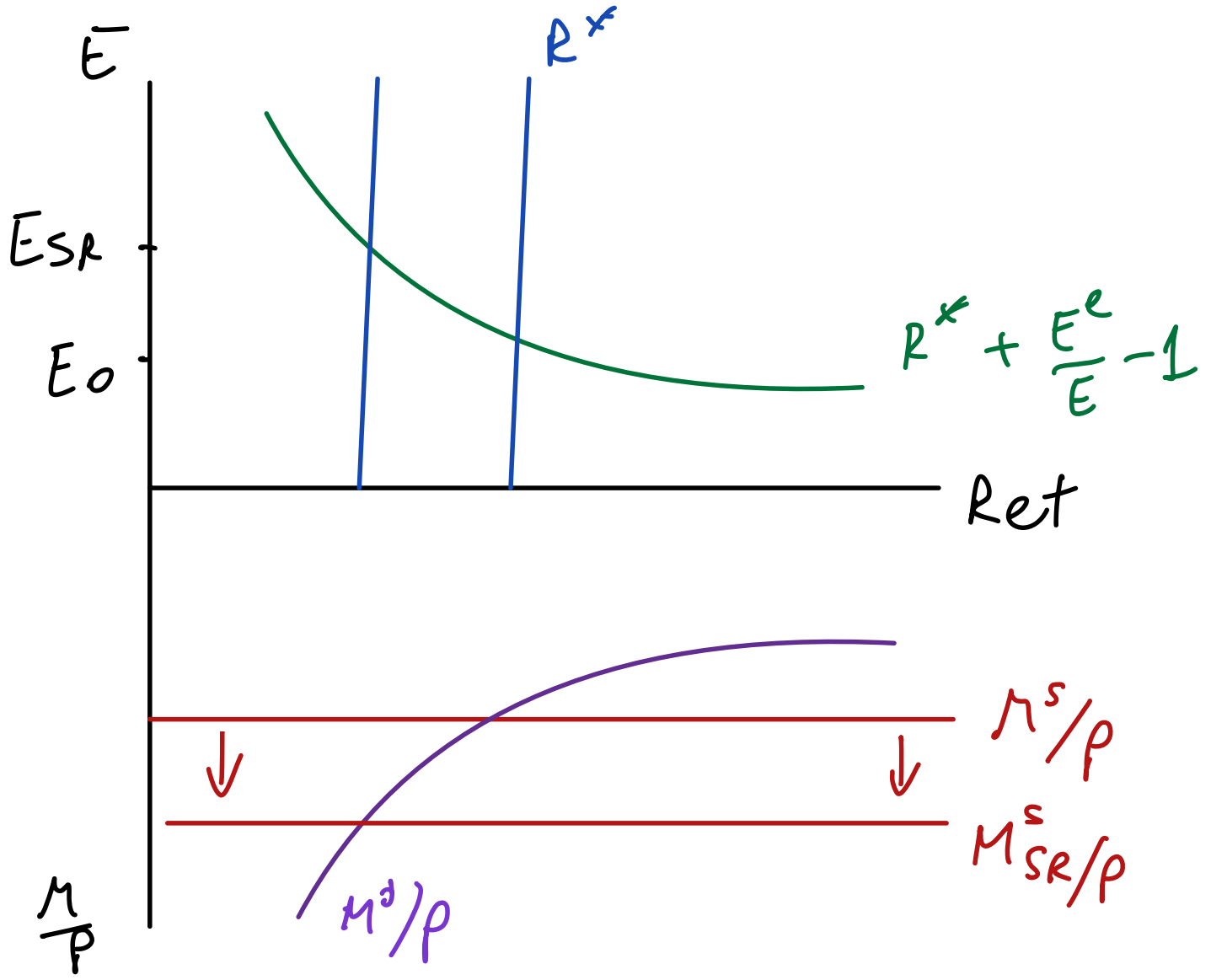
- KEEP LONG RUN  $E$

UNCHANGED  $\Rightarrow$

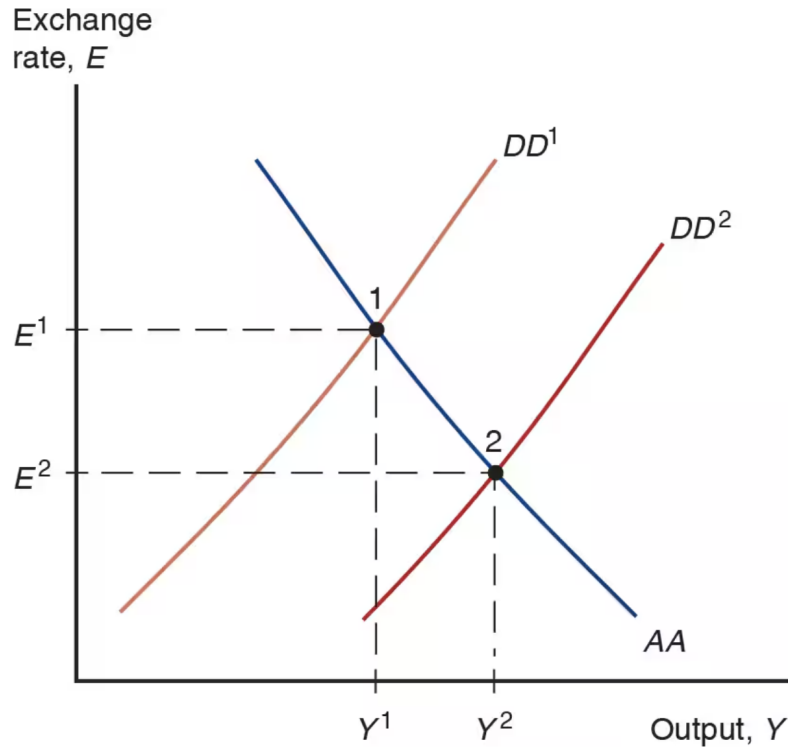
$E_{SR}^e = E_{LR}$  UNCHANGED

- $P_{SR} = P_0$  FIXED

$M^S \uparrow$   
LEADS TO  
 $E \uparrow$



# Temporary Change in Fiscal Policy



GA IN SR ONLY

DA YA FOR ANY E

=> DD SHIFTS TO  
THE RIGHT

# Example: DD Schedule

$$C(Y_D) = 1 + 0.75Y_D$$

(+)

$$EX(q, Y^*) = 0.15 + 0.5q + 0.1Y^*$$

(+)

$$IM(q, Y_D) = 0.1 - 0.2q + 0.12Y_D$$

(-)

$$Y_D = Y - T$$

$$q = \frac{EP^*}{P}$$

- Plug in given  $C$ ,  $EX$ ,  $IM$ ,  $Y_D$ ,  $q$  into the equilibrium condition for the goods market  $Y = C + I + G + EX - IM$  to get:

$$Y = 1.05 + 0.63(Y - T) + 0.7\frac{EP^*}{P} + I + G + 0.1Y^*$$

- Solve for  $E$  to get the DD curve:

$$E = \frac{1}{0.7} \frac{P}{P^*} (-1.05 + 0.37Y + 0.63T - I - G - 0.1Y^*)$$

# Example: AA Schedule

$$R = R^* + \frac{E^e}{E} - 1$$

$$\frac{M^d}{P} = \frac{M^s}{P}$$

$$\frac{M^d}{P} = L\left(\underset{(-)}{R}, \underset{(+)}{Y}\right) = 1.1 - R + 0.05Y$$

- Plug in UIP into money market equilibrium condition:

$$\frac{M^s}{P} = 1.1 - \left(R^* + \frac{E^e}{E} - 1\right) + 0.05Y$$

- Solve for  $E$  to get the AA curve:

$$E = \frac{E^e}{2.1 - \frac{M^s}{P} - R^* + 0.05Y}$$

# Full AA-DD Model

DD Schedule:  $Y = C(Y - T) + I + G + CA(EP^*/P, Y - T, Y^*)$

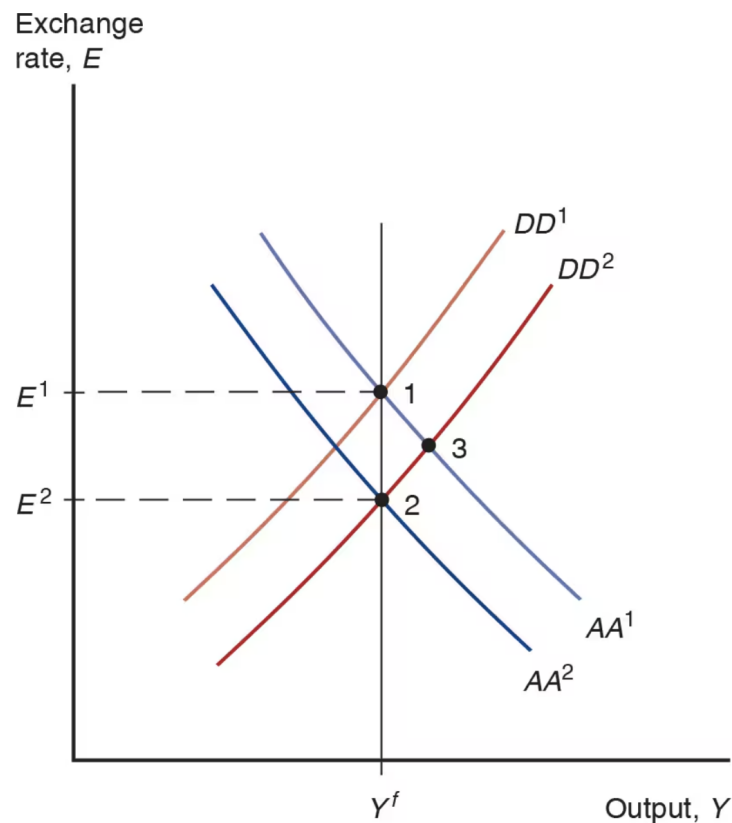
AA Schedule:  $\frac{M^s}{P} = L\left(R^* + \frac{E^e}{E} - 1, Y\right)$

Phillips Curve:  $\pi = \pi^e + \alpha(Y - Y^f)$

Definition of inflation:  $\pi_t = \frac{P_t}{P_{t-1}} - 1$

Definition of expected inflation:  $\pi_t^e = \frac{P_{t+1}^e}{P_t} - 1$

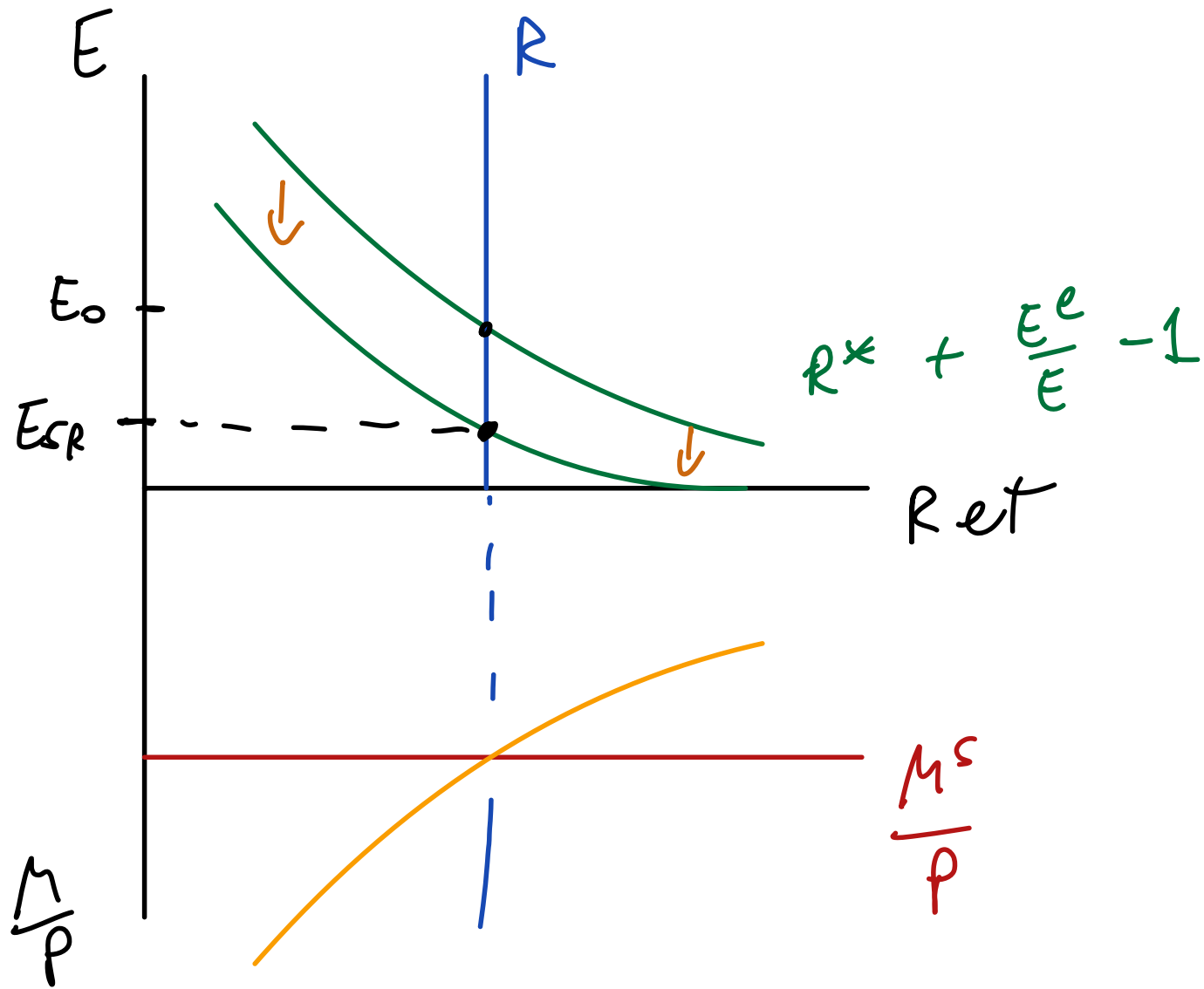
# Permanent Shifts in Fiscal Policy



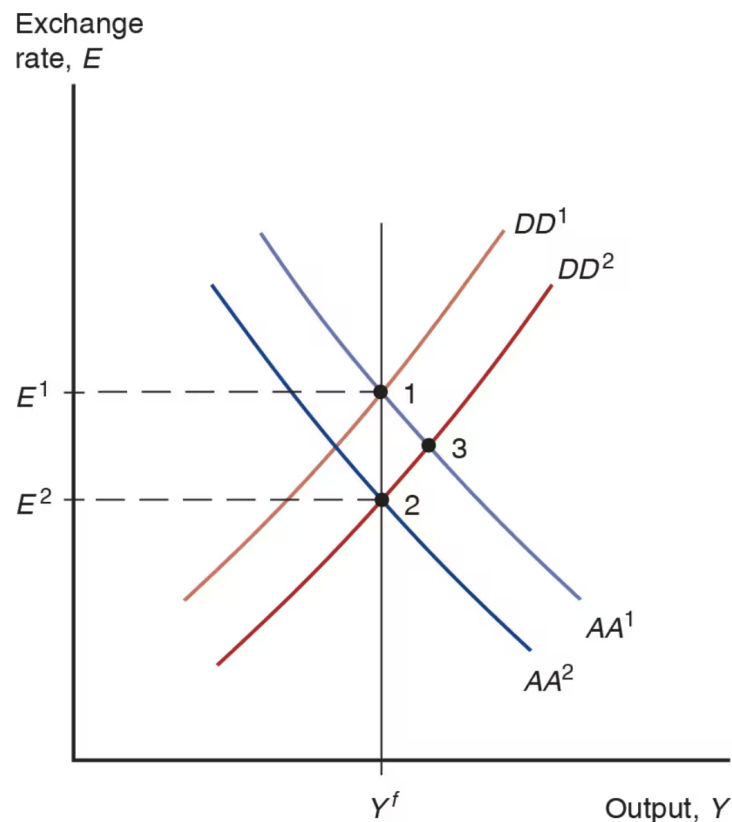
$G \uparrow$  PERMANENTLY

$\Rightarrow D \uparrow \Rightarrow Y \uparrow \Rightarrow DD$  SHIFTS  
TO THE  
RIGHT

$$(AA) : \frac{M^s}{P} = L \left( R^* + \frac{E^e - E}{E}, Y \right)$$

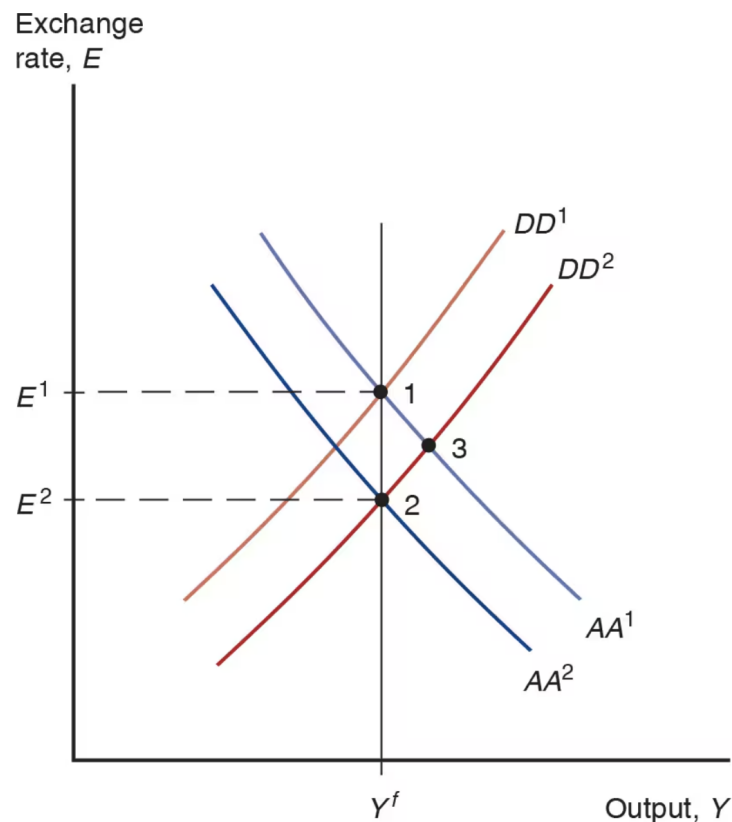


# Permanent Shifts in Fiscal Policy



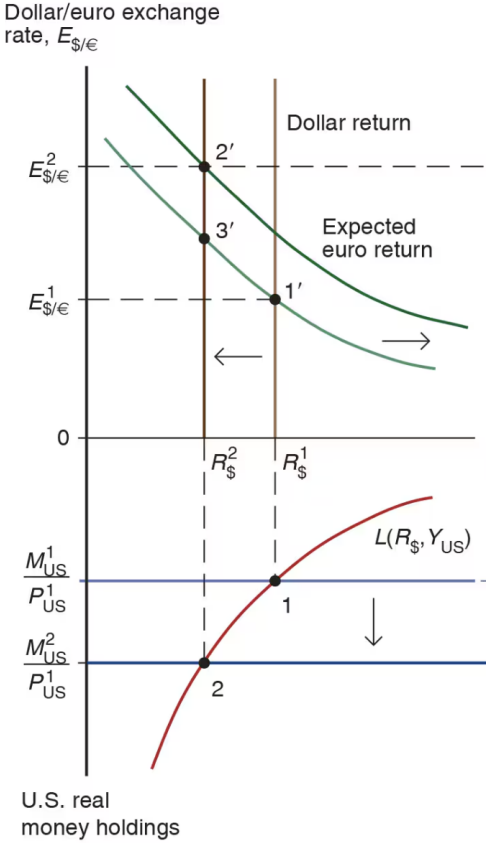
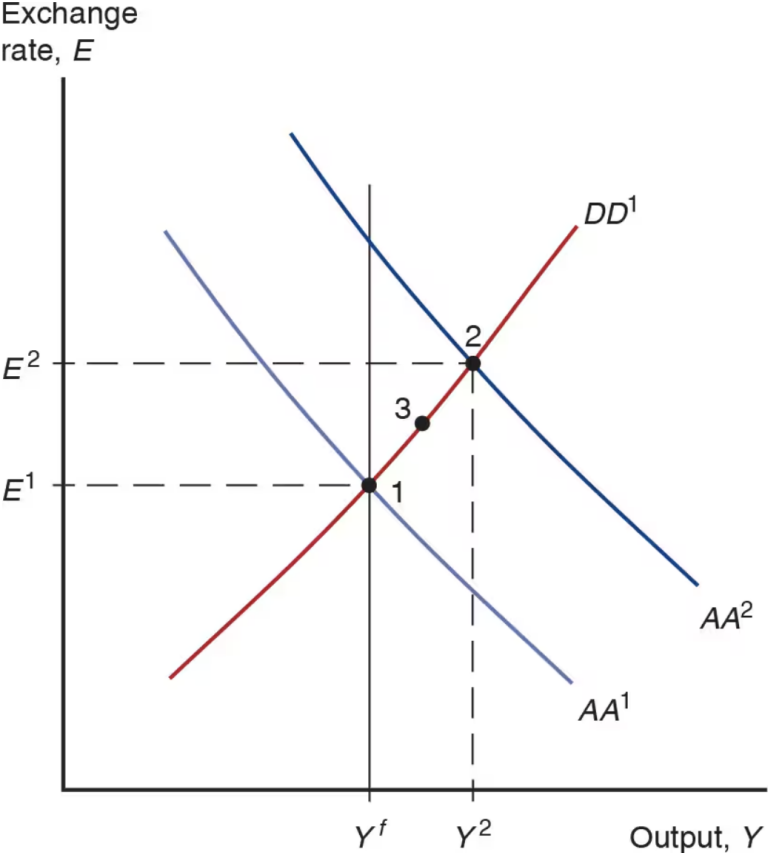
- Start in a medium run equilibrium at point 1 with  $R_0 = R^*$  and  $E_0^e = E^1$
- Increase in  $G$  shifts  $DD$  to the right
- At point 3, exchange rate is lower than  $E_1$
- Since the shift in  $DD$  is permanent, appreciation at point 3 is also expected to be permanent
- $E^e$  must also go down
- Lower  $E^e$  shifts  $AA$  down
- But how much?

# Permanent Shifts in Fiscal Policy



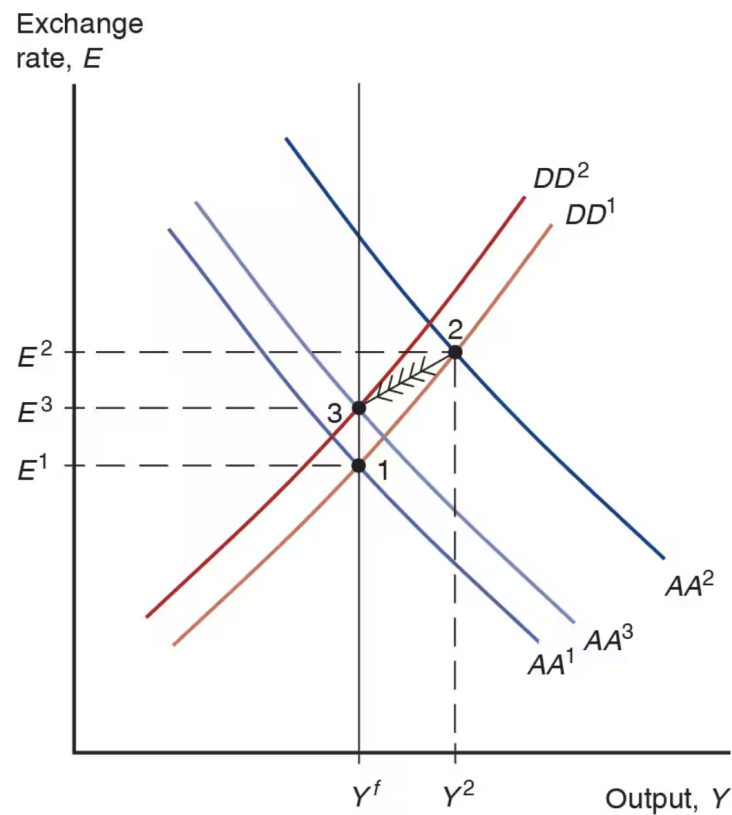
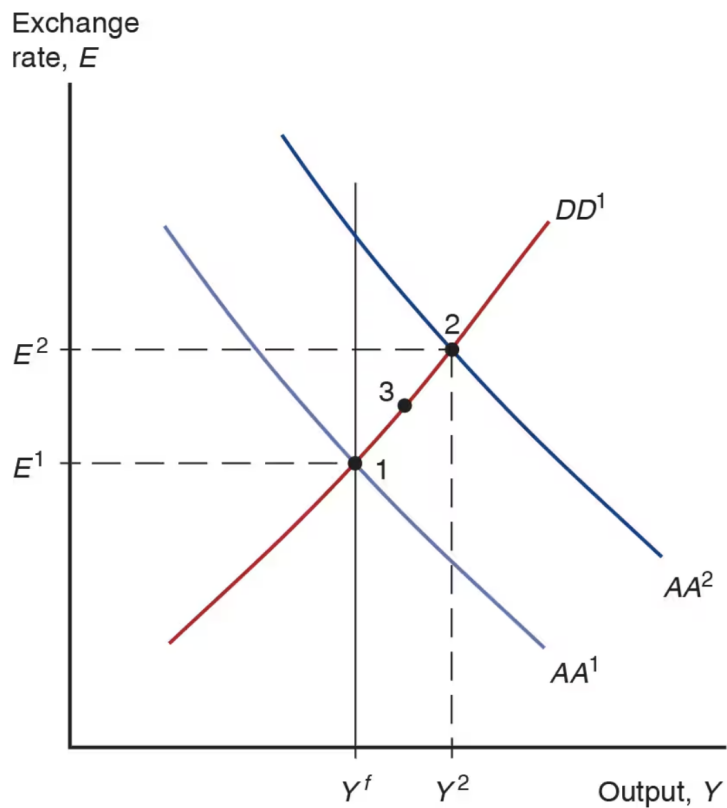
- There are no more shifts expected to occur,  $E^e$  remains constant
- Real money supply is constant
- Long run real money demand must stay unchanged
- Then  $P$  never changes
- $MS=MD$  implies  $R$  does not change
- UIP implies  $E$  does not change either
- If  $Y$  must be equal to its original level  $Y^f$ ,  $AA^1$  must shift to  $AA^2$

# Permanent Shifts in Monetary Policy

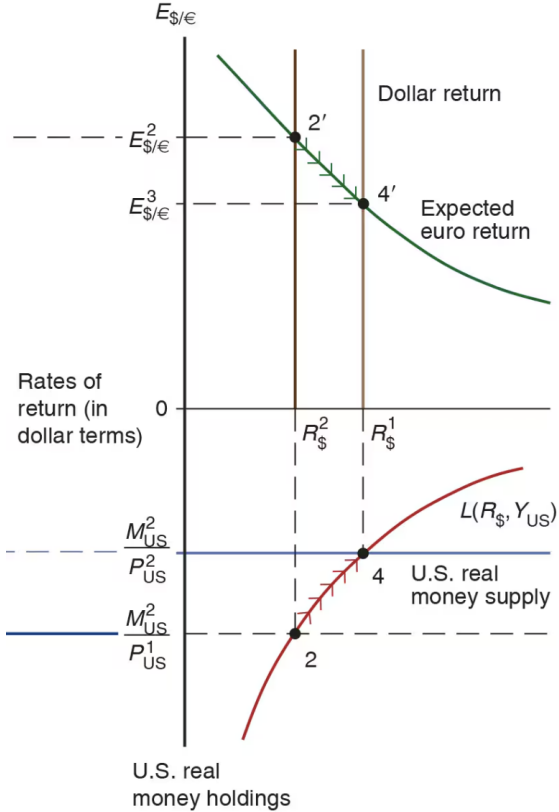
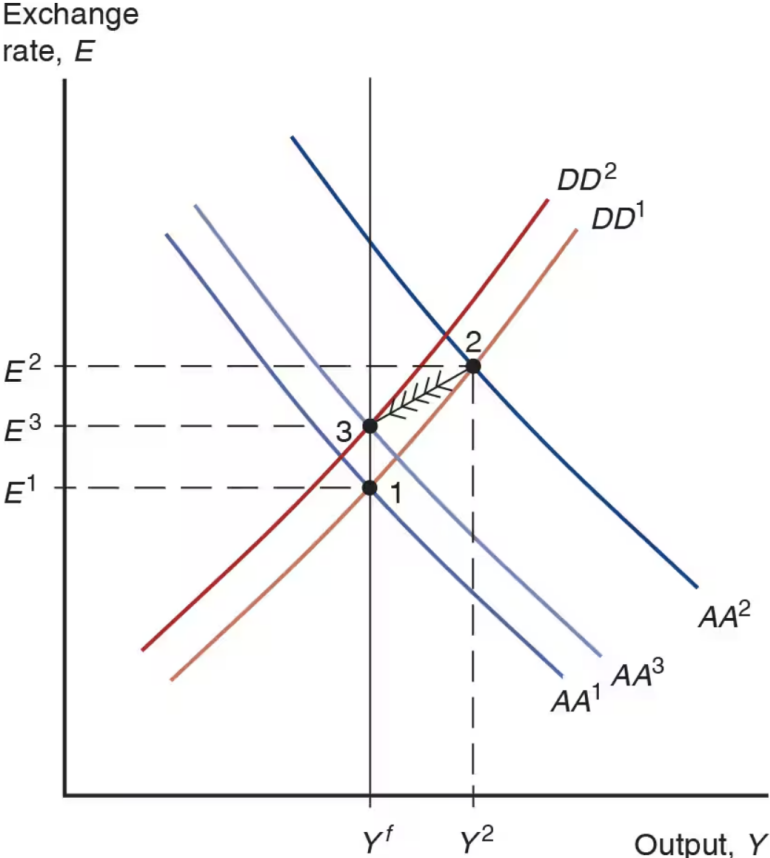


(a) Short-run effects

# Permanent Shifts in Monetary Policy



# Permanent Shifts in Monetary Policy



(b) Adjustment to long-run equilibrium

# DD Schedule with Tariffs

IMPORT TARIFFS - "AD VALOREM" → PROPORTIONAL

$$\begin{array}{l} \text{IM} = q \times \text{VOLUME} \\ \text{UNITS OF DOM GOOD} \quad \downarrow \quad \text{IN UNITS OF FOREIGN GOOD} \\ \text{CHANGE OF UNITS} \end{array} \quad \left| \quad \begin{array}{l} \text{IM}(q, Y-T) \\ \text{(-)} \quad \text{(+)} \\ = q \times \text{VOLUME}(q, Y-T) \\ \text{(-)} \quad \text{(+)} \\ = q \text{ VOLUME}\left(\frac{EP^*}{P}, Y-T\right) \end{array} \right.$$

$$IM = q \times VOLUME \left( \frac{EP^x}{P} (1+\tau), Y-T \right)$$

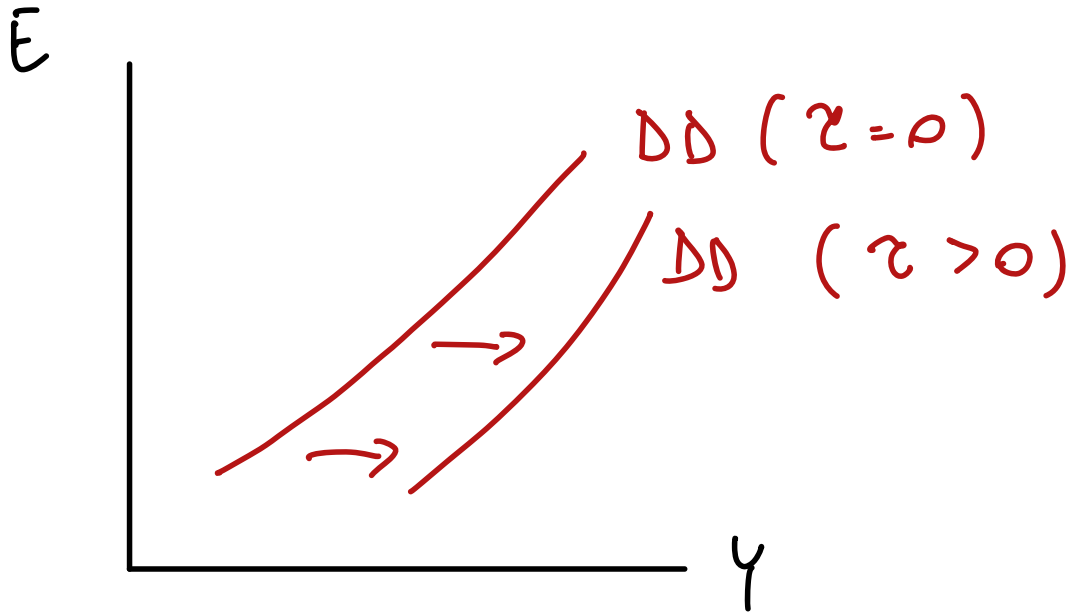
AD VALOREM TARIFF

$$IM = IM \left( q, Y-T, \tau \right)$$

(-)            (+)            (-)

$$Y = C + I + G + EX - IM \left( \tau \right)$$

(-)



DD SHIFTS TO  
THE RIGHT  
WHEN  $z$   
GOES UP